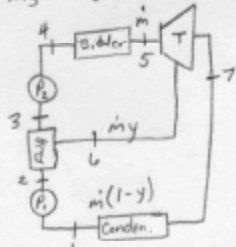


let $y = \frac{m_6}{m_5}$ $y \equiv \% \text{ in feedwater heater (regenerator)}$



Pump
 $\dot{Q}_2 = \Delta KE = \Delta PE = 0$
 $\gamma_p = 1 \Rightarrow s = f$
 $w_2 = -v_1(p_2 - p_1)$
 $w_2 = h_1 - h_2$ $w = \frac{w_2}{\gamma}$

FWH
 $\sum \dot{m}_i h_i = \sum \dot{m}_e h_e$
 let $y = \frac{m_6}{m_5}$
 $\dot{Q} = w = \Delta KE = \Delta PE = 0$

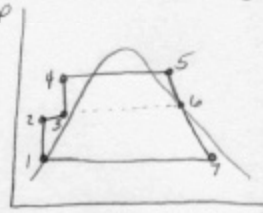
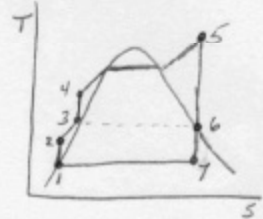
$r_{BW} = \frac{|w_p|}{w_T}$

Boiler
 $\dot{Q}_2 = \Delta KE = \Delta PE = 0$
 $v_2 s = h_2 - h_1$
 lookup s_5

Turbine
 $s_6 = \Delta KE = \Delta PE = 0$
 $\gamma_T = 1 \Rightarrow s = f$
 $s_5 = s_6$
 $s_6 = s_f + x_6 s_{fg}$
 $h_6 = h_f + x_6 h_{fg}$
 $w = w_5 \gamma_T$
 $w = w_5 \gamma_T$

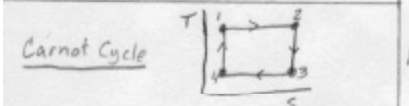
Condenser
 $\dot{Q}_1 = \Delta KE = \Delta PE = 0$
 $\dot{Q}_1 = h_1 - h_7$

Reheater
 $w = \Delta KE = \Delta PE = 0$
 $\gamma_{th} = \frac{w_{net}}{\dot{Q}_{in}}$
 assume SSSF
 $\dot{W} = \dot{m} w_{net}$ (no FWH)



Ways to increase η_{th}	+	-
1. Reduce Condenser Press.	$\eta_{th} \uparrow$	$x \downarrow$ erodes turbine
2. Increase boiler temp.	$\eta_{th} \uparrow, x \uparrow$	
3. Increase boiler press.	$\eta_{th} \uparrow$	$x \downarrow$
4. Reduce condenser temp.	$\eta_{th} \uparrow$	$x \downarrow$
5. Increase turbine inlet temp.	$\eta_{th} \uparrow$	$x \downarrow$ % reheat

- Deviations from ideal rankine cycle**
1. pressure drop in piping
 2. pressure drop in condenser, boiler
 3. heat transfer from pipes
 4. turbine, pump $\Rightarrow \eta_{th} \neq 1$

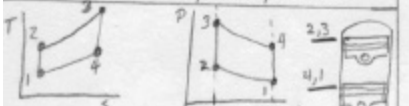


Process 1-2: isothermal expansion
 $\Delta KE = \Delta PE = 0$, closed system
 $T_1 = T_2$

Process 2-3: isentropic expansion

Process 3-4: isothermal heat rejection

Process 4-1: isentropic compression



Otto Cycle (closed system)

Process 1-2: Isentropic compression
 $\Delta KE = \Delta PE = 0, \dot{Q}_2 = 0$
 $v_2 = v_1 r_v^{k-1}$
 $\dot{Q}_2 = u_1 - u_2 = C_v(T_1 - T_2)$
 $\frac{P_2}{P_1} = (r_v)^k$; $r_v \equiv \frac{v_1}{v_2}$; $\frac{T_2}{T_1} = (r_v)^{k-1}$

Process 2-3: $\dot{Q} = \dot{Q}_{in}$ heat addition
 $\dot{Q}_3 = 0 = \Delta KE = \Delta PE$
 $\frac{P_3}{P_2} = r_v^k$; $\frac{P_3}{P_1} = \frac{T_3}{T_2}$

Process 3-4: $s = f$ expansion
 $\dot{Q}_4 = \Delta KE = \Delta PE = 0$
 $\frac{T_4}{T_3} = \left(\frac{1}{r_v}\right)^{k-1}$

Process 4-1: $\dot{Q} = \dot{Q}_{out}$ heat rejection
 $\Delta KE = \Delta PE = 0$
 $\dot{Q}_1 = u_4 - u_1 = C_v(T_4 - T_1)$
 $\eta_{th} = 1 - \frac{\dot{Q}_1}{\dot{Q}_2}$
 $mep = \frac{w_{net}}{v_1 - v_2}$

To use r_v & PR exponentiated terms, must be $\pm G, C_p = k, s = f$

Dual cycle rejects more heat if $r_v \& PR \Rightarrow \eta_{th}$ the same

Diesel/Otto comparison:
 * If r_v same, $\dot{Q}_2 \uparrow, \eta_{th} \downarrow$
 * Can obtain same \dot{Q}_{in} by compression
 * $r_v \uparrow, \eta_{th} \uparrow$ in diesel compress air
 * no auto-ignite.
 * Can't compress Otto because of auto-ignite.
 * mep for diesel & Otto because fuel must be at high P & ignite, so limited time for burn
 * In Otto, P can be lower

Otto cycle: - good mep
 - η_{th} reasonable
 - must set P_{max}, T_{max} for dependability
 - $\eta_{th} = 1 - \frac{1}{r_v^k - 1}$ for ideal case
 - $r_v \uparrow, \eta_{th} \uparrow, T_{max} \uparrow$
 - actual operation: knock if $r_v \uparrow$
 - $\dot{Q} = \dot{Q}_{burn}$ unobtainable so $\dot{Q}_2 \downarrow, \eta_{th} \downarrow$
 - expansion is cooled
 - pumping losses occur
 - open valve before BDC: lose work

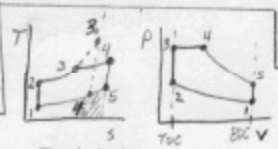
Diesel cycle:
 - if r_v same, $(\eta_{th})_D > (\eta_{th})_O$
 - don't have to worry about auto-ignite
 * $(r_v)_D > (r_v)_O \Rightarrow (\eta_{th})_D > (\eta_{th})_O$
 - regulate power by amount of fuel (fuel doesn't burn @ low P)
 * $(mep)_O > (mep)_D$

Otto: mep better
 $\eta_{th} < \eta_{th}$ of diesel at steady operating conditions

Carnot Engines: highest η_{th} size & dependability negate high η_{th}

$\dot{Q}_{in} = \dot{P}_{in} \left(\frac{V_{piston}}{R_s} \right) T = \frac{\dot{W}_{net}}{2\pi R_s}$

$\dot{Q}_{in} = \dot{Q}_{DC} - \dot{Q}_{TC}$
 R_s - rotational speed (RPs)
 n - # strokes related to input of mass
 $n = 2$ (4-stroke)
 $n = 1$ (2-stroke)
 $\eta_{th} = 1 - \frac{\dot{Q}_1}{\dot{Q}_2}$



Dual Cycle

Process 1-2: $s = f$ compression
 $\frac{T_2}{T_1} = (r_v)^{k-1}$
 $\frac{P_2}{P_1} = (r_v)^k$

Process 2-3: $v = f$ heat addition
 $P_3 = P_2 \frac{T_3}{T_2}$

Process 3-4: $P = f$
 $\dot{Q}_4 = u_4 - u_3 + \dot{Q}_4$
 $\dot{Q}_4 = P(v_4 - v_3) = \int P dv$
 $\dot{Q}_4 = (u_4 + P_4 v_4) - (u_3 + P_3 v_3)$
 $\dot{Q}_4 = h_4 - h_3 \approx C_p(T_4 - T_3)$

Process 4-5: $s = f$ expansion
 $\frac{v_4}{v_3} = \frac{T_4}{T_3}$
 $\frac{v_5}{v_4} = \frac{r_v}{T_4/T_3}^{k-1}$
 $T_5 = T_4 \left(\frac{v_5}{v_4} \right)^{k-1}$

Process 5-1: $\dot{Q} = \dot{Q}_{out}$ heat rejection
 $\dot{Q}_1 = \Delta KE = \Delta PE = 0$
 $\dot{Q}_1 = u_1 - u_5 = C_v(T_1 - T_5)$
 $\eta_{th} = 1 - \frac{\dot{Q}_1}{\dot{Q}_2}$
 $mep = \frac{w_{net}}{v_1 - v_2}$

Diesel Cycle

Process 1-2: $s = f$ compression
 $\Delta KE = \Delta PE = 0, \dot{Q}_2 = 0$
 $\frac{T_2}{T_1} = (r_v)^{k-1}$
 $\frac{P_2}{P_1} = (r_v)^k$

Process 2-3: $P = f$ heat addition
 $\dot{Q}_3 = u_3 - u_2 + \dot{Q}_3$
 $\dot{Q}_3 = \int P dv = P(v_3 - v_2)$
 $\dot{Q}_3 = (u_3 + P v_3) - (u_2 + P v_2)$
 $\dot{Q}_3 = h_3 - h_2$
 $r_c \equiv \frac{v_3}{v_2}$ (fuel cutoff ratio)
 $\frac{P_2}{P_3} = \frac{RT_2}{RT_3} = \frac{P_3}{P_2} = \frac{T_2}{T_3} \Rightarrow r_c = \frac{T_3}{T_2}$

Process 3-4: $s = f$ expansion
 $\frac{T_4}{T_3} = \left(\frac{v_4}{v_3} \right)^{k-1}$ don't calc. work
 $\frac{P_4}{P_3} = \left(\frac{v_4}{v_3} \right)^k$
 $\frac{v_4}{v_3} = \frac{r_v}{r_c}$

Process 4-1: $\dot{Q} = \dot{Q}_{out}$ heat rejection
 $\dot{Q}_1 = u_1 - u_4$
 $\eta_{th} = 1 - \frac{\dot{Q}_1}{\dot{Q}_2}$
 $\eta_{th} = 1 - \frac{1}{(r_v)^{k-1}} \left[\frac{r_c^k - 1}{k} \right]$
 $w_{net} = \eta_{th} \cdot \dot{Q}_2$
 $mep = \frac{w_{net}}{v_1 - v_2}$
 $w_{net} \neq w_2 + w_4$ because there is w_3

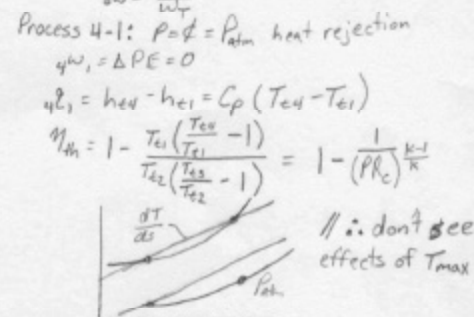
Brayton Cycle (turbine engine)

Process 1-2: $\dot{Q}_2 = \Delta PE = 0$
 $\dot{Q}_2 = h_2 + \frac{v_2^2}{2} + g z_2 - h_1 - \frac{v_1^2}{2} - g z_1 + \dot{Q}_2$
 isentropic compression (stagnation)
 $\dot{Q}_2 = h_2 + \frac{v_2^2}{2} + g z_2 + \dot{Q}_2$
 cold air I.R.
 $\dot{Q}_2 = C_p(T_2 - T_1)$
 $C_p T_2 = C_p T_1 + \frac{v_2^2}{2}$
 $PR_c = \frac{P_2}{P_1} = \frac{P_2}{P_1} = \frac{P_2}{P_1}$
 $\left(\frac{P_2}{P_1} \right)^{\frac{k-1}{k}} = \frac{T_2}{T_1}$; $P_2 = P_1 (PR_c)^{\frac{k}{k-1}}$

Process 2-3: $P = f$ heat addition, SSSF
 $\Delta PE = \dot{Q}_3 = 0$
 $\dot{Q}_3 = -\int v dp \Rightarrow \dot{Q}_3 = 0$
 $\dot{Q}_3 = \int T ds$
 $\dot{Q}_3 = h_3 - h_2 = C_p(T_3 - T_2)$

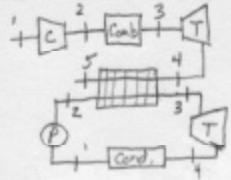
Process 3-4: isentropic compression
 $\dot{Q}_4 = \Delta PE = 0$
 $\dot{Q}_4 = C_p(T_4 - T_3)$
 $s = f, k = f, I.R.$
 $PR_c = \frac{P_3}{P_4}$; $T_4 = T_3 \left(\frac{1}{PR_c} \right)^{\frac{k-1}{k}}$
 $r_{BW} = \frac{w_c}{w_T}$

Process 4-1: $P = f = P_{atm}$ heat rejection
 $\dot{Q}_1 = \Delta PE = 0$
 $\dot{Q}_1 = h_4 - h_1 = C_p(T_4 - T_1)$
 $\eta_{th} = 1 - \frac{T_4(T_1 - T_3)}{T_2(T_3 - T_1)} = 1 - \frac{1}{(PR_c)^{\frac{k}{k-1}}}$



Brayton Cycle
 power to weight ratio superior
 $(\eta_{th})_B < (\eta_{th})_O$
 $\eta_{th} = 1 - \frac{1}{(PR)^{\frac{k}{k-1}}}$ (ideal only)
 if $PR_c \uparrow, \eta_{th} \uparrow$ (limited PR)
 if $T_{max} \uparrow, \eta_{th} \uparrow$
 sees T_{max} all times, limited $T_{max} \uparrow$
 can add regeneration cycle if $T_{re} > T_{c1}$

Co-Generation cycle



Comp. T_c must be \leq Turb. T_e

Process 1-2: Comp. (G.T.)

$$w_{cs} = (h_{e2s} - h_{e1s})$$

$$w_c = \frac{w_{cs}}{\eta_c} = h_{e2} - h_{e1}$$

Process 2-3: $P = \text{const}$ comb. (G.T.)

$$z_2 p_2 = z_3 p_3 = h_{e3} - h_{e2}$$

Process 3-4: expansion (G.T.)

$$P_{r4s} = P_{r3} \left(\frac{P_4}{P_3} \right)$$

$$w_{T3} = h_{u4s} - h_{e3}$$

$$w_T = w_{T3} \cdot \eta_{T3} = h_{e4} - h_{e3}$$

Process 1-2: Pump (R)

$$w_{ps} = v_f (P_2 - P_1)$$

$$w_p = \frac{w_{ps}}{\eta_p} = h_2 - h_1$$

Process 2-3: heat exchanger

$$z_2 p_2 = z_3 p_3 = \Delta KE = \Delta PE = 0$$

$$\sum \dot{m}_i h_i = \sum \dot{m}_e h_e$$

$$\dot{m}_{st} (h_3 - h_2) = \dot{m}_g (h_{e4} - h_{e3})$$

Process 3-4: Turbine (R)

$$w_{T3} = h_3 - h_{4s}, s_3 = s_{4s} \Rightarrow x_4$$

$$h_{4s} = h_f + x_4 h_{fg}$$

$$w_T = w_{T3} \cdot \eta_T$$

$$\dot{w} = \dot{m}_g (w_{net})_{GT} + \dot{m}_{st} (w_{net})_R$$

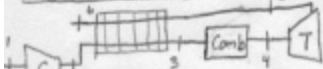
$$\frac{\dot{m}_{st}}{\dot{m}_g} = \frac{h_{e4} - h_{e3}}{h_3 - h_2}$$

$$\dot{w} = \dot{m}_g (w_{net})_{GT} + \left(\frac{\dot{m}_{st}}{\dot{m}_g} \right) (w_{net})_R$$

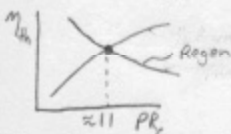
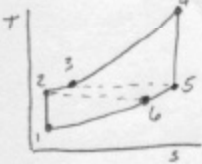
$$\eta_{th} = \frac{\dot{w}_{net}}{\dot{Q}_H}$$

$$\dot{Q}_H = \dot{m}_{AT} (z_2 p_2)_{GT}$$

Regenerative cycle



$$\eta_R = \frac{h_3 - h_2}{h_5 - h_2} = \frac{T_{e3} - T_{e2}}{T_{e5} - T_{e2}} \text{ if } C_p = \text{const}$$



Jet Propulsion

Diffuser: $w = 0$

$$h_1 + \frac{V_1^2}{2} = h_2 + \frac{V_2^2}{2} = h_{e2}$$

$$C_p T_1 + \frac{V_1^2}{2} = C_p T_2 + \frac{V_2^2}{2}$$

$$\dot{m}_1 = \dot{m}_2 \text{ solve for } V_2$$

$$P_1 A_1 V_1 = P_2 A_2 V_2$$

$$P_1 = P_2 R T$$

$$A_1 = \frac{\dot{m}}{\rho_1 V_1}$$

$$\frac{P_2}{P_1} = \left(\frac{T_2}{T_1} \right)^{\frac{k-1}{k}}$$

$$T_{e2} = T_2 + \frac{V_2^2}{2 C_p}$$

Compressor $w = 0$ s=f

$$w_{cs} = h_{e3} - h_{e2}$$

$$T_{e3} = T_{e2} \cdot (P_{r3})^{\frac{k-1}{k}}$$

Combustor $w = 0$ P=f

$$P_{e3} = P_{e4}$$

$$P = h_{e4} - h_{e3}$$

Turbine $w = 0$ s=f

$$w = h_{e4} - h_{e5}$$

$$\frac{P_{e5}}{P_{e4}} = \left(\frac{T_{e5}}{T_{e4}} \right)^{\frac{k-1}{k}}$$

Nozzle

$$P_b = P_1$$

$$\frac{T_b}{T_{e5}} = \left(\frac{P_b}{P_{e5}} \right)^{\frac{k-1}{k}}$$

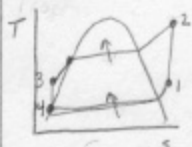
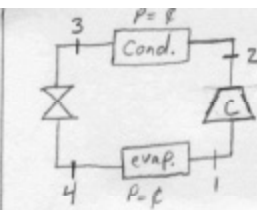
$$C_p T_{b5} + \frac{(V_{b5})^2}{2} = C_p T_{e5}$$

$$V_b = \sqrt{\eta_n \cdot (V_{b5})^2}$$

$$\text{Thrust} = \dot{m} (V_b - V_1)$$

$$\eta_{PR} = \frac{(\text{thrust}) V_1}{\dot{Q}_H \cdot \dot{m}}$$

$$\frac{1}{C} \frac{1}{T} \frac{1}{P}$$



Process 1-2 s=f comp

$$\dot{w} = \dot{m} (h_1 - h_{2s}) / \eta_c$$

Process 3-4 s=f

$$s_4 = s_{2s} = 0$$

$$\therefore h_3 = h_4$$

$$h_3 = h_{r@T_3}$$

$$\dot{Q}_L = \dot{m} (h_1 - h_4)$$

$$\beta = \frac{\dot{Q}_L}{\dot{w}_{in}}$$

$$y_i = \frac{n_i}{n_m} \left(\frac{\text{kmol}}{\text{kmol}} \right)$$

$$m_i = M_i y_i \left(\frac{\text{kg}}{\text{kmol}} \right)$$

$$m_m = \sum M_i y_i$$

$$m f_i = \frac{m_i}{m_m}$$

$$y_i = \frac{P_i}{P_m}$$

$$M_m = \sum m_i y_i$$

$$(n_i = \frac{m_i}{M_i})$$

$$\bar{C}_p = C_p M$$

$$\bar{C}_p = \sum y_i \bar{C}_{pi}$$

$$P V_m = M_m R_m T_m$$

$$R_m = \frac{R}{M_m}$$

$$\dot{m} = \frac{\dot{V}}{V}$$

Given $(k_g) m$

$$n_i = \frac{m_i}{M_i}$$

$$y_i = \frac{n_i}{n_m}$$

Compression Ratios

$$\frac{T_2}{T_1} = (r_v)^{k-1} \quad \text{I.G., } C_p = \text{const}$$

$$\frac{P_2}{P_1} = (r_v)^k$$

$$\frac{T_2}{T_1} = \left(\frac{1}{r_v}\right)^{k-1} \quad \text{I.G., expansion}$$

Pressure Ratios

$$\frac{T_2}{T_1} = \left(\frac{1}{PR_c}\right)^{\frac{k-1}{k}}$$

$$\frac{P_2}{P_1} = \frac{1}{PR_c}$$

$$PR \equiv \frac{P_1}{P_2}$$

$$V_1 = \frac{V_2}{m}$$

$$C_p T_{e2} = C_p T_1 + \frac{V_1^2}{2}$$

$$1 \text{ kJ} = 1000 \text{ kg m}^2/\text{s}^2$$

$$f = \frac{1}{V}$$

$$C_p - C_v = R$$

$$\frac{C_p}{C_v} = k$$

Heat Pump

$$\alpha = \frac{Q_h}{W_{net}} = \frac{Q_h}{Q_h - Q_L} \quad \text{heat}$$

$$\beta = \frac{Q_L}{W_{net}} = \frac{Q_L}{Q_h - Q_L} \quad \text{AC}$$

$$\alpha - \beta = 1$$

$$W_{net} = Q_h - Q_L$$

$$211 \text{ kJ/min} = 1 \text{ ton}$$

Throttling

$$T = \text{const}$$

$$h = \text{const}$$

not reversible

$$Q + \sum m_i \left[u_i + \frac{V_i^2}{2} + g z_i \right] = W + \sum m_e \left[u_e + \frac{V_e^2}{2} + g z_e \right] \quad \boxed{\text{closed system}}$$

$$W = \int P dv + \frac{V_e^2 - V_i^2}{2} + g(z_e - z_i) \quad \boxed{\text{closed system reversible}}$$

$$Q + \sum m_i \left[h_i + \frac{V_i^2}{2} + g z_i \right] = W + \sum m_e \left[h_e + \frac{V_e^2}{2} + g z_e \right] \quad \boxed{\text{steady flow}}$$

$$W = - \int v dP - \frac{V_e^2 - V_i^2}{2} - g(z_e - z_i) \quad \boxed{\text{reversible steady flow}}$$

$$Q = \int T ds \quad \boxed{\text{reversible}}$$

$$\dot{m}_1 = \dot{m}_2 + \dot{m}_3$$

$$\dot{m}_1 = \dot{m}_2 + \dot{m}_3$$

$$\dot{m}_1 = \dot{m}_2 + \dot{m}_3$$

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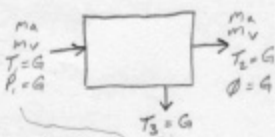
$$\dot{m}_1 = \dot{m}_2 + \dot{m}_3$$

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$$\dot{m}_1 = \dot{m}_2 + \dot{m}_3$$

$$\dot{m}_1 = \dot{m}_2 + \dot{m}_3$$



$$\dot{V} = V \cdot A$$

$$\dot{m} = \rho \dot{V}$$

$$V = \frac{\dot{V}}{A}$$

$$r_{bw} = \frac{w_c}{w_T}$$

$$T_3 = T_2 + \frac{2P_3}{C_v}$$

$$\phi_1 = \frac{P_{v1}}{P_g @ T_1}$$

$$P_{v1} = \phi_1 P_g @ T_1$$

$$\omega_1 = 0.622 \left(\frac{P_{v1}}{P_{m1} - P_{v1}} \right)$$

$$P_{v2} = \phi_2 P_g @ T_2$$

$$\omega_2 = 0.622 \left(\frac{P_{v2}}{P_{m2} - P_{v2}} \right)$$